

**Prof. Dr. Alfred Toth**

## **Relationalzahlen topologischer semiotischer Relationen II**

1. Die in Toth (2019a) definierten 6 möglichen Einbettungsstufen 1. Stufe logisch-semiotisch-ontischer Relationen lassen sich mit Hilfe von Relationalzahlen (vgl. Toth 2015) wie folgt definieren

$$R = (A, B) = (1, 2)$$

$$R = ((A, B)) = ((1, 2)_{-1})$$

$$R = ((A), B) = (1_{-1}, 2)$$

$$R = (B, (A)) = (2, 1_{-1})$$

$$R = ((B), A) = (2_{-1}, 1)$$

$$R = (B, (A)) = (2, 1_{-1}).$$

Die 6 mal  $36 = 216$  durch E differenzierbaren topologischen semiotischen Relationen, d.h. das vollständige System einer topologischer dyadisch-trichotomischen Semiotik, lässt sich hernach wie folgt formal darstellen.

$$(1.1, 2.1) \quad (1.1_{-1}, 2.1) \quad (1.1, 2.1_{-1}) \quad (2.1_{-1}, 1.1) \quad (2.1, 1.1_{-1}) \quad ((2.1, 1.1)_{-1})$$

$$(1.1, 2.1] \quad (1.1_{-1}, 2.1] \quad (1.1, 2.1_{-1}] \quad (2.1_{-1}, 1.1] \quad (2.1, 1.1_{-1}] \quad ((1.1, 2.1)_{-1}]$$

$$[1.1, 2.1) \quad [1.1_{-1}, 2.1) \quad [1.1, 2.1_{-1}) \quad [2.1_{-1}, 1.1) \quad [2.1, 1.1_{-1}) \quad [(1.1, 2.1)_{-1})$$

$$[1.1, 2.1] \quad [1.1_{-1}, 2.1] \quad [1.1, 2.1_{-1}] \quad [2.1_{-1}, 1.1] \quad [2.1, 1.1_{-1}] \quad [(1.1, 2.1)_{-1}]$$

$$(1.1, 2.2) \quad (1.1_{-1}, 2.2) \quad (1.1, 2.2_{-1}) \quad (2.2_{-1}, 1.1) \quad (2.2, 1.1_{-1}) \quad ((1.1, 2.2)_{-1})$$

$$(1.1, 2.2] \quad (1.1_{-1}, 2.2] \quad (1.1, 2.2_{-1}] \quad (2.2_{-1}, 1.1] \quad (2.2, 1.1_{-1}] \quad ((1.1, 2.2)_{-1}]$$

$$[1.1, 2.2) \quad [1.1_{-1}, 2.2) \quad [1.1, 2.2_{-1}) \quad [2.2_{-1}, 1.1) \quad [2.2, 1.1_{-1}) \quad [(1.1, 2.2)_{-1})$$

$$[1.1, 2.2] \quad [1.1_{-1}, 2.2] \quad [1.1, 2.2_{-1}] \quad [2.2_{-1}, 1.1] \quad [2.2, 1.1_{-1}] \quad [(1.1, 2.2)_{-1}]$$

$$(1.1, 2.3) \quad (1.1_{-1}, 2.3) \quad (1.1, 2.3_{-1}) \quad (2.3_{-1}, 1.1) \quad (2.3, 1.1_{-1}) \quad ((1.1, 2.3)_{-1})$$

$$(1.1, 2.3] \quad (1.1_{-1}, 2.3] \quad (1.1, 2.3_{-1}] \quad (2.3_{-1}, 1.1] \quad (2.3, 1.1_{-1}] \quad ((1.1, 2.3)_{-1}]$$

|            |                           |                           |                           |                           |                             |
|------------|---------------------------|---------------------------|---------------------------|---------------------------|-----------------------------|
| [1.1, 2.3) | [1.1 <sub>-1</sub> , 2.3) | [1.1, 2.3 <sub>-1</sub> ) | [2.3 <sub>-1</sub> , 1.1) | [2.3, 1.1 <sub>-1</sub> ) | [(1.1, 2.3) <sub>-1</sub> ) |
| [1.1, 2.3] | [1.1 <sub>-1</sub> , 2.3] | [1.1, 2.3 <sub>-1</sub> ] | [2.3 <sub>-1</sub> , 1.1] | [2.3, 1.1 <sub>-1</sub> ] | [(1.1, 2.3) <sub>-1</sub> ] |
| (1.2, 2.1) | (1.2 <sub>-1</sub> , 2.1) | (1.2, 2.1 <sub>-1</sub> ) | (2.1 <sub>-1</sub> , 1.2) | (2.1, 1.2 <sub>-1</sub> ) | ((1.2, 2.1) <sub>-1</sub> ) |
| (1.2, 2.1] | (1.2 <sub>-1</sub> , 2.1] | (1.2, 2.1 <sub>-1</sub> ] | (2.1 <sub>-1</sub> , 1.2] | (2.1, 1.2 <sub>-1</sub> ] | ((1.2, 2.1) <sub>-1</sub> ] |
| [1.2, 2.1) | [1.2 <sub>-1</sub> , 2.1) | [1.2, 2.1 <sub>-1</sub> ) | [2.1 <sub>-1</sub> , 1.2) | [2.1, 1.2 <sub>-1</sub> ) | [(1.2, 2.1) <sub>-1</sub> ) |
| [1.2, 2.1] | [1.2 <sub>-1</sub> , 2.1] | [1.2, 2.1 <sub>-1</sub> ] | [2.1 <sub>-1</sub> , 1.2] | [2.1, 1.2 <sub>-1</sub> ] | [(1.2, 2.1) <sub>-1</sub> ] |
| (1.2, 2.2) | (1.2 <sub>-1</sub> , 2.2) | (1.2, 2.2 <sub>-1</sub> ) | (2.2 <sub>-1</sub> , 1.2) | (2.2, 1.2 <sub>-1</sub> ) | ((1.2, 2.2) <sub>-1</sub> ) |
| (1.2, 2.2] | (1.2 <sub>-1</sub> , 2.2] | (1.2, 2.2 <sub>-1</sub> ] | (1.2 <sub>-1</sub> , 2.2] | (1.2, 2.2 <sub>-1</sub> ] | ((1.2, 2.2) <sub>-1</sub> ] |
| [1.2, 2.2) | [1.2 <sub>-1</sub> , 2.2) | [1.2, 2.2 <sub>-1</sub> ) | [2.2 <sub>-1</sub> , 1.2) | [2.2, 1.2 <sub>-1</sub> ) | [(1.2, 2.2) <sub>-1</sub> ) |
| [1.2, 2.2] | [1.2 <sub>-1</sub> , 2.2] | [1.2, 2.2 <sub>-1</sub> ] | [2.2 <sub>-1</sub> , 1.2] | [2.2, 1.2 <sub>-1</sub> ] | [(1.2, 2.2) <sub>-1</sub> ] |
| (1.2, 2.3) | (1.2 <sub>-1</sub> , 2.3) | (1.2, 2.3 <sub>-1</sub> ) | (2.3 <sub>-1</sub> , 1.2) | (2.3, 1.2 <sub>-1</sub> ) | (1.2, 2.3) <sub>-1</sub> )  |
| (1.2, 2.3] | (1.2 <sub>-1</sub> , 2.3] | (1.2, 2.3 <sub>-1</sub> ] | (2.3 <sub>-1</sub> , 1.2] | (2.3, 1.2 <sub>-1</sub> ] | ((1.2, 2.3) <sub>-1</sub> ] |
| [1.2, 2.3) | [1.2 <sub>-1</sub> , 2.3) | [1.2, 2.3 <sub>-1</sub> ) | [2.3 <sub>-1</sub> , 1.2) | [2.3, 1.2 <sub>-1</sub> ) | [(1.2, 2.3) <sub>-1</sub> ) |
| [1.2, 2.3] | [1.2 <sub>-1</sub> , 2.3] | [1.2, 2.3 <sub>-1</sub> ] | [2.3 <sub>-1</sub> , 1.2] | [2.3, 1.2 <sub>-1</sub> ] | [(1.2, 2.3) <sub>-1</sub> ] |
| (1.3, 2.1) | (1.3 <sub>-1</sub> , 2.1) | (1.3, 2.1 <sub>-1</sub> ) | (2.1 <sub>-1</sub> , 1.3) | (2.1, 1.3 <sub>-1</sub> ) | ((1.3, 2.1) <sub>-1</sub> ) |
| (1.3, 2.1] | (1.3 <sub>-1</sub> , 2.1] | (1.3, 2.1 <sub>-1</sub> ] | (2.1 <sub>-1</sub> , 1.3] | (2.1, 1.3 <sub>-1</sub> ] | ((1.3, 2.1) <sub>-1</sub> ] |
| [1.3, 2.1) | [1.3 <sub>-1</sub> , 2.1) | [1.3, 2.1 <sub>-1</sub> ) | [2.1 <sub>-1</sub> , 1.3) | [2.1, 1.3 <sub>-1</sub> ) | [(1.3, 2.1) <sub>-1</sub> ) |
| [1.3, 2.1] | [1.3 <sub>-1</sub> , 2.1] | [1.3, 2.1 <sub>-1</sub> ] | [2.1 <sub>-1</sub> , 1.3] | [2.1, 1.3 <sub>-1</sub> ] | [(1.3, 2.1) <sub>-1</sub> ] |
| (1.3, 2.2) | (1.3 <sub>-1</sub> , 2.2) | (1.3, 2.2 <sub>-1</sub> ) | (2.2 <sub>-1</sub> , 1.3) | (2.2, 1.3 <sub>-1</sub> ) | ((1.3, 2.2) <sub>-1</sub> ) |
| (1.3, 2.2] | (1.3 <sub>-1</sub> , 2.2] | (1.3, 2.2 <sub>-1</sub> ] | (2.2 <sub>-1</sub> , 1.3] | (2.2, 1.3 <sub>-1</sub> ] | ((1.3, 2.2) <sub>-1</sub> ] |
| [1.3, 2.2) | [1.3 <sub>-1</sub> , 2.2) | [1.3, 2.2 <sub>-1</sub> ) | [2.2 <sub>-1</sub> , 1.3) | [2.2, 1.3 <sub>-1</sub> ) | [(1.3, 2.2) <sub>-1</sub> ) |
| [1.3, 2.2] | [1.3 <sub>-1</sub> , 2.2] | [1.3, 2.2 <sub>-1</sub> ] | [2.2 <sub>-1</sub> , 1.3] | [2.2, 1.3 <sub>-1</sub> ] | [(1.3, 2.2) <sub>-1</sub> ] |

|              |                   |                   |                   |                   |                      |
|--------------|-------------------|-------------------|-------------------|-------------------|----------------------|
| $(1.3, 2.3)$ | $(1.3_{-1}, 2.3)$ | $(1.3, 2.3_{-1})$ | $(2.3_{-1}, 1.3)$ | $(2.3, 1.3_{-1})$ | $((1.3, 2.3)_{-1})$  |
| $(1.3, 2.3]$ | $(1.3_{-1}, 2.3]$ | $(1.3, 2.3_{-1}]$ | $(2.3_{-1}, 1.3]$ | $(2.3, 1.3_{-1}]$ | $((1.3, 2.3)_{-1}]$  |
| $[1.3, 2.3)$ | $[1.3_{-1}, 2.3)$ | $[1.3, 2.3_{-1})$ | $[2.3_{-1}, 1.3)$ | $[2.3, 1.3_{-1})$ | $[(1.3, 2.3)_{-1})$  |
| $[1.3, 2.3]$ | $[1.3_{-1}, 2.3]$ | $[1.3, 2.3_{-1}]$ | $[2.3_{-1}, 1.3]$ | $[2.3, 1.3_{-1}]$ | $[(1.3, 2.3)_{-1}].$ |

2. Wie man leicht zeigen kann, liegen den 6 durch E differenzierbaren topologischen semiotischen Relationen nur 3 geometrische Darstellungen ihrer zahlentheoretischen Strukturen zu Grunde

$(w.x), (y.z)$

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— — — — — .

$(w.x), (y.z)$

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$(y.z)$



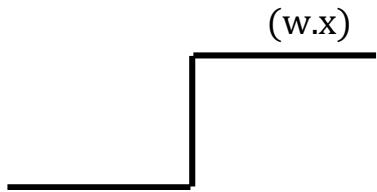
$(w.x)$

$(w.x)$

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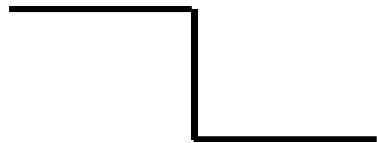


$(y.z)$



(y.z)

(y.z)



(w.x)

Wir haben also die 3 folgenden geometrischen Basisstrukturen

$(A, B), ((A, B)_{-1})$



$B/A$



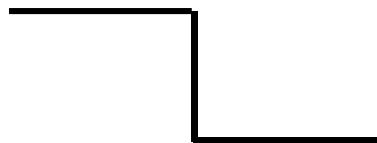
$(A_{-1}, B)$

$A/B$

$(A, B_{-1})$

$B/A$

$(B_{-1}, A)$



$(B, A_{-1})$

$B/A$

## Literatur

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